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**NOTE:** The numbering of equations, exercises, tables, and figures is described on page 27 (footnote), page 29 (footnote), and page 74.

Latin and Greek symbols are listed in the index, the latter in the alphabetical order of their English names.

Mathematical symbols not admitting of alphabetical listing are grouped in the index under the heading 'symbols.'