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## **Preface**

Chapters 1–11 were written by Zeev B. Alfassi, chapter 12 was written by Yigal Ronen, and chapter 13 was written by Zvi Boger.

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