620.101 HEA

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Answers to exercises are available on the Internet at:
http://www.ncl.ac.uk/~nengm/publish/